

A photograph of two black dice and several playing cards on a green felt surface. The dice are in the foreground, showing different faces with white pips. Behind them are several playing cards, including the Ace of Spades, King of Spades, Queen of Spades, Jack of Spades, and Ten of Spades. The Ace of Spades is prominently displayed on the right, showing its intricate design. A blue banner with white text is in the upper left, and the title 'Topic 22: Probability(4048)' is in the lower right.

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## Topic 22: Probability(4048)



THE ABOUT

# CHAPTER ANALYSIS



MASTERY

- Conceptually simple chapter, but can be deceptively difficult and complicated
- 3 **key** concepts



EXAM

- Concepts usually tested as a stand-alone topic
- Easy to make careless mistakes if not careful i.e. under/double counting



WEIGHTAGE

- High overall weightage
- Tested consistently every year
- Typically, an 8m question, 1-2 questions in one of the papers

KEY CONCEPT

# Probability

## Possibility Diagram & Tree Diagram

### Addition & Multiplication Laws

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### Unique Properties of Probabilities

Event	Probability
Sample space consisting of $N$ possible outcomes that are equally likely	$\frac{1}{N}$
Outcome of an event is not possible	0
Outcome of an event is definitely going to happen	1

## Probability

Branch of Mathematics that deals with calculating the likelihood of a given event's occurrence, always expressed as a number between 0 and 1

$$\text{Probability of } \underbrace{P(\text{rolling a 6 on a fair dice})}_{\text{Event's occurrence}} = \frac{1}{6}$$

Calculate probabilities using the following expression:

$$P(\text{Event}) = \frac{\text{Number of favourable outcomes}}{\text{Total number of possible outcomes}}$$





## Possibility Diagram

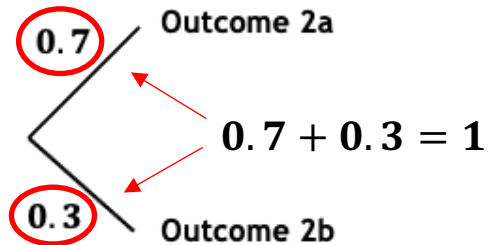
Diagram which shows all possible outcomes of an experiment, usually used where each outcome is equally likely to happen

Example: Sum of 2 dices thrown

		First Dice					
Second Dice	+	1	2	3	4	5	6
	1	2	3	4	5	6	7
	2	3	4	5	6	7	8
	3	4	5	6	7	8	9
	4	5	6	7	8	9	10
	5	6	7	8	9	10	11
	6	7	8	9	10	11	12

**Take note:**

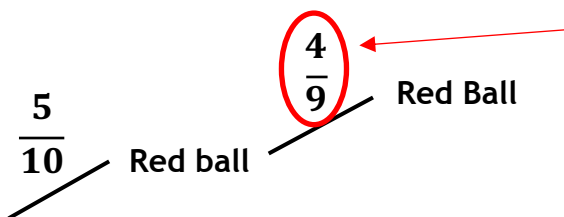
Probability of every completed branch must add up to 1

**Common Mistake / Examination Phrase:**

“ ... taken out of the bag without replacement ... ”

This means that the object is taken out of the bag, and not placed back inside, this in-turn will change the outcome of the resultant probability

EX: 5 red balls out of 10 balls, 2 balls taken out without replacement



Why  $\frac{4}{9}$ ?

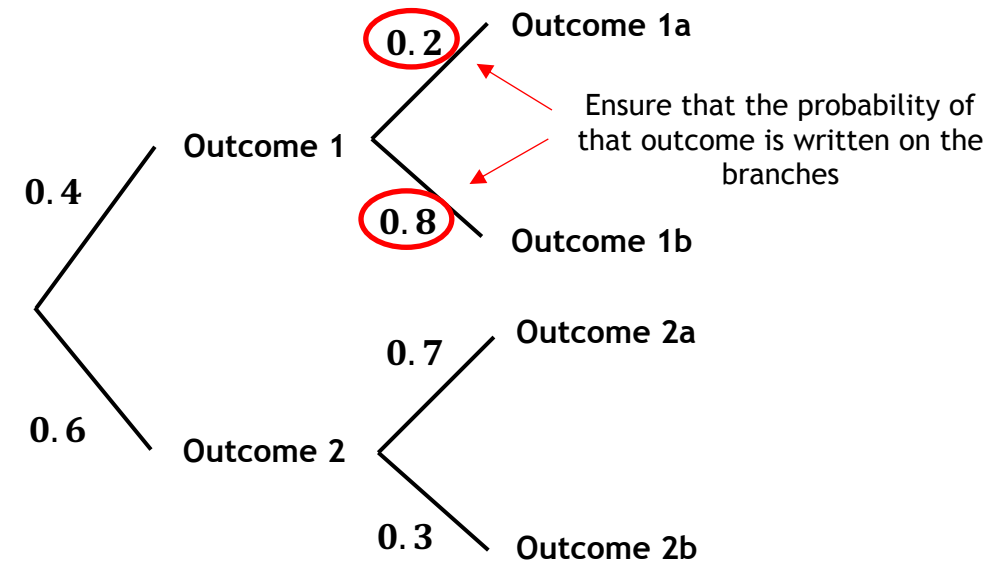
Since there is no replacement, and the first ball taken out is red, there are 9 balls remaining, 4 of which are red

**Tree Diagram**

Each of the  $n_1$  ways to completing the first outcome is represented as the branch of the tree diagram

Each of the ways to completing the second outcome is represented as  $n_2$  branches from the ends of the original branches and so on...

Example:







## Addition & Multiplication Laws

### 1. Addition Law

Applies for 2 or more mutually exclusive events. When 2 events are mutually exclusive, it means that they cannot happen at the same time

$$P(A \text{ or } B) = P(A \cup B) = P(A) + P(B)$$

### 2. Multiplication Law

Applies for 2 or more independent events. When 2 events are independent, it means that the occurrence of one of them has no influence on the occurrence of the other

$$P(A \text{ and } B) = P(A \cap B) = P(A) \times P(B)$$

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