

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021



**OVERMUGGED MOCK PAPER 2021  
SECONDARY 4 EXPRESS  
SECONDARY 5 NORMAL ACADEMIC**

**ADDITIONAL MATHEMATICS**

**4049/01**

**Specimen Paper**

**Date: 1 September 2021**

**Duration: 2 hours 15 minutes**

**Candidates answer on separate writing paper**

---

**READ THESE INSTRUCTIONS FIRST**

Write your name on all work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

You are expected to use a scientific calculator to evaluate explicit numerical expressions.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures.

Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value of **3.142**, unless the question requires the answer in terms of  $\pi$ .

At the end of the exam, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question

The total number of marks for this paper is **90**.

Setter: Ong Kai Wen

**This question paper consists of 18 printed pages including the cover page**

## **MATHEMATICAL FORMULAE**

---

### 1. ALGEBRA

#### *Quadratic Equation*

For the equation  $ax^2 + bx + c = 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

#### *Binomial expansion*

$$(a + b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n,$$

where  $n$  is a positive integer and  $\binom{n}{r} = \frac{n!}{r!(n-r)!} = \frac{n(n-1)\dots(n-r+1)}{r!}$

### 2. TRIGONOMETRY

#### *Identities*

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A = 2 \cos^2 A - 1 = 1 - 2 \sin^2 A$$

$$\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$

#### *Formulae for $\triangle ABC$*

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2}bc \sin A$$

1. In view of a contagious virus, the government of a particular country has imposed a ‘Stay-Home-Notice’ on her people to reduce the number of human-to-human transmission cases. It is estimated that the percentage of the population,  $P$ , complying to the Stay-Home-Notice is given by the following equation, where  $t$  is the number of days after the imposition

$$P = 100(1 - e^{-0.15t})$$

- (a) Find the percentage of population complying to the ‘Stay-Home-Notice’ after 5 days of the imposition

[1]

- (b) Find the number of complete days after the imposition that it will take for at least 90% of the population to comply

[2]

- (c) Is It possible for the percentage of this country’s population complying to the ‘Stay-Home-Notice’ to reach 100%. Explain your answer

[1]

[S4 ZHSS P1/2020 PRELIM Qn 4]

[Total: 4 marks]

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

2. It is given that the following line meets the curve, where  $k$  is a constant.

$$y = 2x - 3k + 3$$

$$y = x^2 - kx + k^2$$

Find the smallest and largest possible of  $k$

[5]

[S4 YISS P1/2020 PRELIM Qn 2]

[Total: 5 marks]

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

3. Evaluate the following

$$\int \frac{x^2 + 7}{(x - 3)(x + 1)^2} dx$$

[Hint: Split the fraction using Partial Fractions]

[8]

[S4 YSS P1/2020 PRELIM Qn 7 (Modified)]

[Total: 8 marks]

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

4. Find the value of each of the constants  $A$  and  $B$  given the following equations

$$y = \frac{1}{2}(e^{2x} + 5e^{-2x})$$
$$\frac{d^2y}{dx^2} - \frac{dy}{dx} = Ae^{2x} + Be^{-2x}$$

[4]

[S4 TSS P1/2020 PRELIM Qn 3]

[Total: 4 marks]

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

5. Given that  $\log_2 a = h$  and  $\log_2 b = k$ , express the following in terms of  $h$  and  $k$

$$\log_2 \sqrt{\frac{32a}{b^3}}$$

[4]

[S4 SMSS P1/2020 PRELIM Qn 4]

[Total: 4 marks]

6. (a) A trigonometric function is defined by the following for  $0^\circ \leq x \leq 360^\circ$

$$f(x) = 2 - 3 \cos x$$

- (i) State the amplitude of the graph of  $y = f(x)$

[1]

- (ii) State the period of the graph of  $y = f(x)$

[1]

- (b) Another trigonometric function, where  $a < 0$ , has a maximum value of 5, a minimum value of  $-1$  and a period of  $540^\circ$

$$g(x) = a \sin\left(\frac{x}{b}\right) + c$$

Find the values of  $a$ ,  $b$  and  $c$

[3]



Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

(c) On the same diagram, sketch the graphs of  $y = f(x)$  and  $y = g(x)$  for  $0^\circ \leq x \leq 360^\circ$

[4]

(d) State the number of solutions of

$$a \sin\left(\frac{x}{b}\right) + 3 \cos x + c = 2$$

[1]

[S4 JSS P1/2020 PRELIM Qn 12]

[Total: 10 marks]

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

7. The equation of a curve is  $y = x^3 + kx^2 - 3x + 1$ , where  $k$  is a constant

(a) Find, in terms of  $k$ , the gradient of tangent to the curve at the point  $x = 1$

[2]

(b) Explain why the curve has two stationary points, for any real values of  $k$

[3]

(c) If  $k = -4$ , find the range of values of  $x$  for which  $y$  is a decreasing function

[2]

[S4 SST P1/2020 PRELIM Qn 5]

[Total: 7 marks]

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

8. In the following expansion, where  $m$  is a positive constant, the term independent of  $x$  is **61236**

$$\left(x^2 + \frac{m}{x}\right)^9$$

- (a) Show that  $m = 3$

[4]

- (b) Hence or otherwise, find the coefficient of  $x^6$  in the expansion of

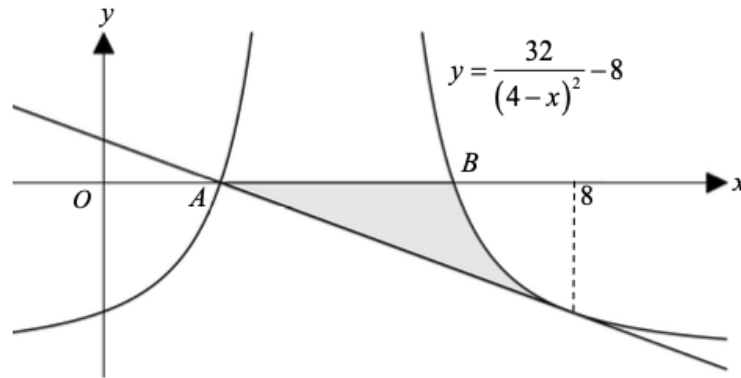
$$(2 - 5x^3)\left(x^2 + \frac{3}{x}\right)^9$$

[4]

[S4 PCSS P1/2020 PRELIM Qn 6]

[Total: 8 marks]

9.



The diagram shows part of the curve, intersecting the  $x$ -axis at  $A$  and  $B$

$$y = \frac{32}{(4-x)^2} - 8$$

The tangent to the curve at  $x = 8$  meets the  $x$ -axis at  $A$

(a) Find the equation of the tangent

[4]

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

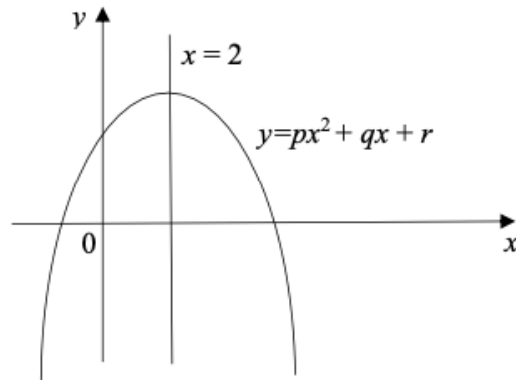
(b) Find the area of the shaded region

[6]

[S4 NHHS P1/2020 PRELIM Qn 10]

[Total: 10 marks]

10.



The diagram above shows part of the graph of

$$y = px^2 + qx + r$$

The equation of the line of symmetry of the curve is  $x = 2$ . Determine the conditions for each of the following expressions, justifying your answer

(a)

$$q^2 - 4pr$$

[2]

(b)

$$\frac{dy}{dx} \text{ when } x = 2$$

[2]

(c)

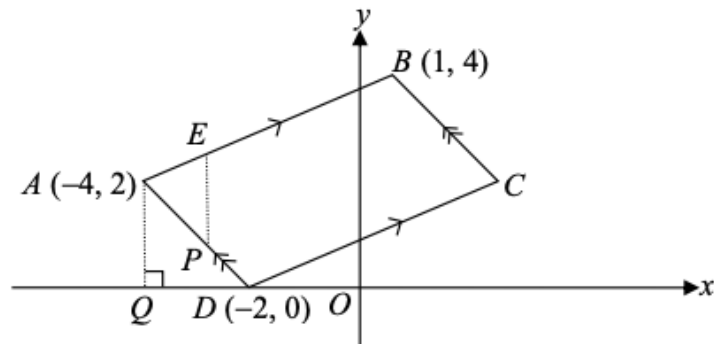
$$q$$

[2]

[S4 MGS P1/2020 PRELIM Qn 10]

[Total: 6 marks]

11. Solutions to this question by accurate drawing will not be accepted



$ABCD$  is a parallelogram where  $A$  is  $(-4, 2)$ ,  $B$  is  $(1, 4)$  and  $D$  is  $(-2, 0)$ . The point  $E$  lies on  $AB$  such that  $AE:EB = 2:5$ . Lines are drawn, parallel to the  $y$ -axis, from  $A$  to meet the  $x$ -axis at  $Q$  and from  $E$  to meet  $AD$  at  $P$

(a) Calculate the coordinates of  $C$  and of  $E$

[4]

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

(b) Find the equation of  $AD$  and calculate the coordinates of  $P$

[3]

(c) Explain why  $AEPQ$  is a parallelogram and calculate its area

[3]

[S4 MSS P1/2020 PRELIM Qn 12]

[Total: 10 marks]



Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

12. The acute angles  $A$  and  $B$  are such that

$$\tan(A + B) = 8$$

$$\tan A = \frac{1}{5}$$

Without using a calculator, find the exact value of

$$\cos B$$

[5]

[S4 JWSS P1/2020 PRELIM Qn 2]

[Total: 5 marks]

Name: \_\_\_\_\_

Material: A-Math Mock Paper 2021

13. A company manufactures aluminium beverage cans and the design of the can is modelled using a right cylindrical can of radius  $r$  cm and height  $h$  cm. Each can needs to hold at least  $355 \text{ cm}^3$  of liquid. The company would like to minimise the area of the aluminium sheet used for each can. Using suitable calculations, advise the company of the dimensions of the can.

[Hint: State the appropriate height and radius of the can]

[9]

[S4 NGHS P1/2020 PRELIM Qn 12]

[Total: 9 marks]

End of Paper 😊